



# A Comprehensive Multiphysics Model for Organic Photovoltaics

**Zi Shuai Wang, Wei E. I. Sha, and Wallace C. H. Choy**

**Presenter: Wei E. I. Sha**

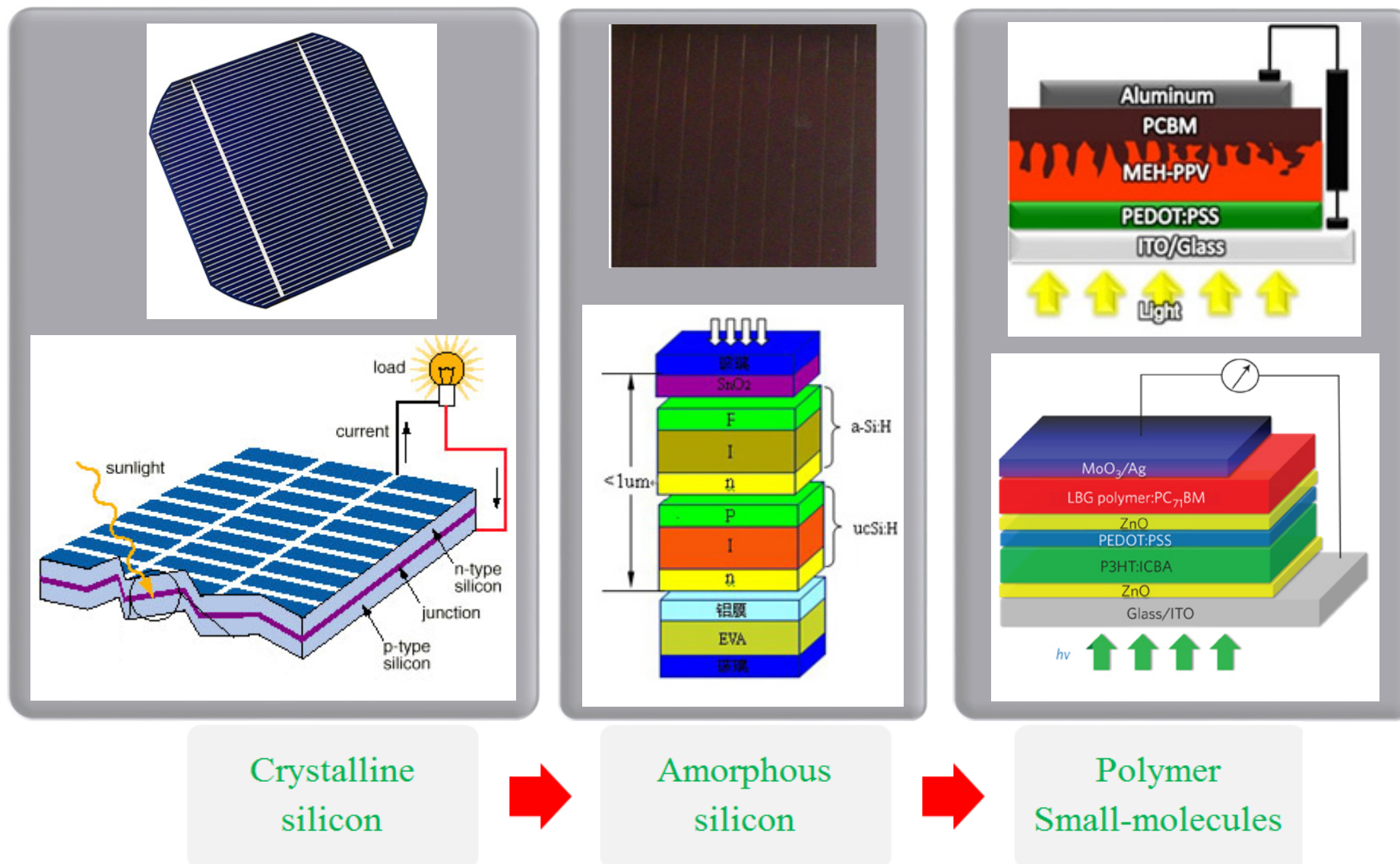
**Email: [wsha@eee.hku.hk](mailto:wsha@eee.hku.hk)**

**Website: <http://www.eee.hku.hk/~wsha>**

**Department of Electrical and Electronic Engineering  
The University of Hong Kong, Hong Kong**

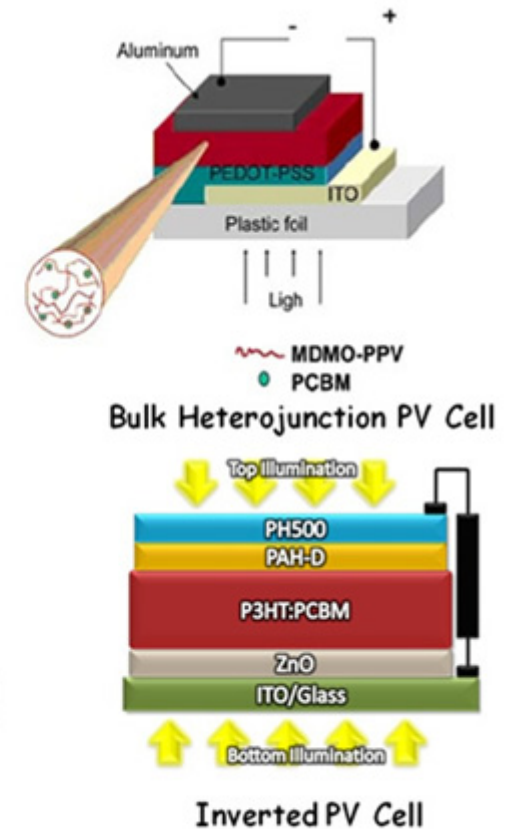
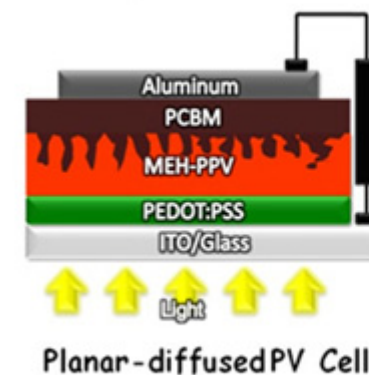
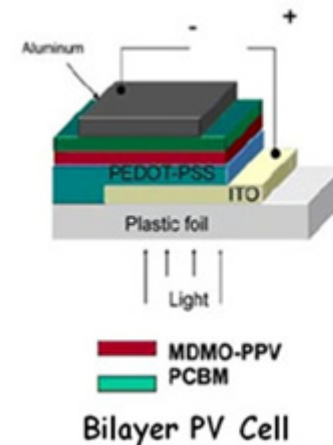
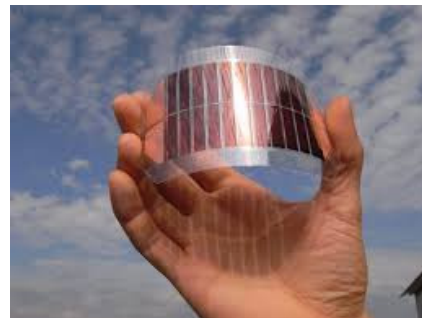


# ADVANCES OF SOLAR CELL TECHNOLOGY

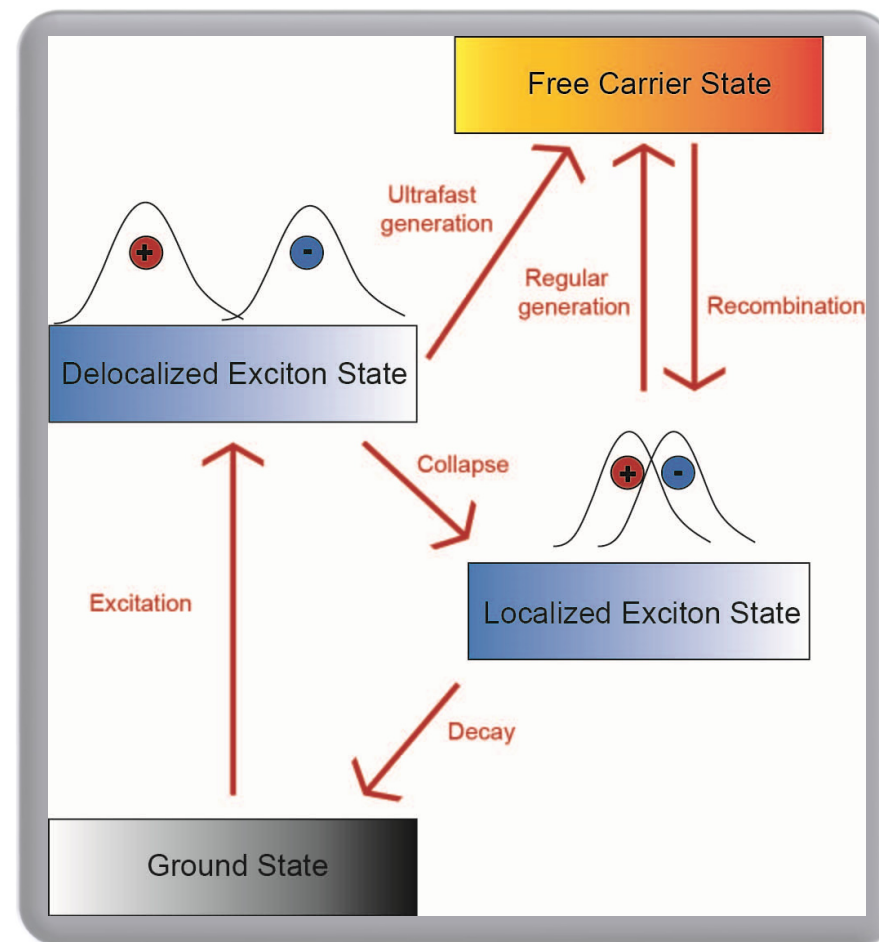
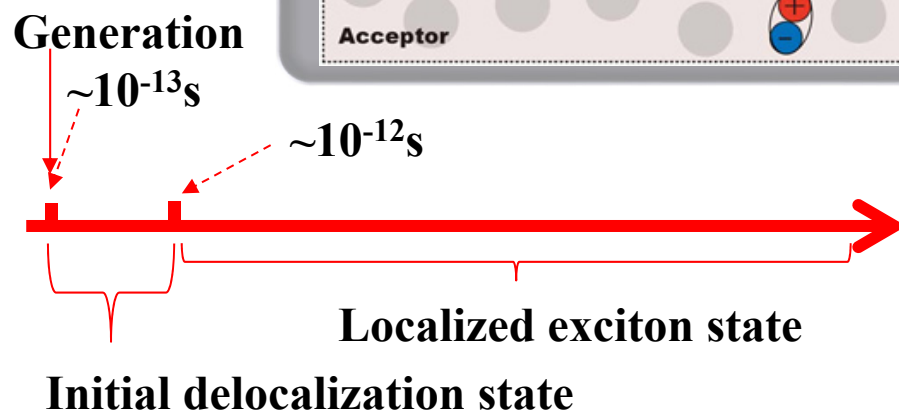
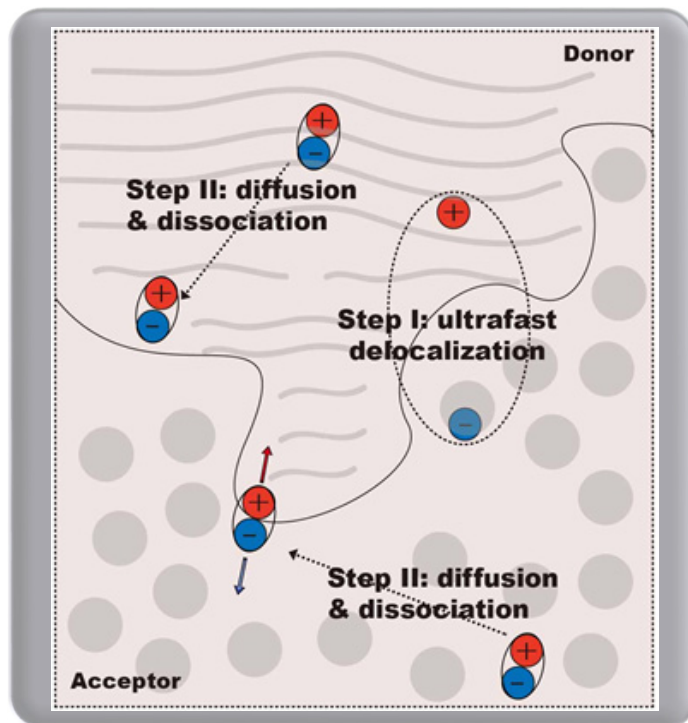


# PROPERTIES OF ORGANIC SOLAR CELLS

- ✓ *low-cost processing*
- ✓ *mechanically flexible*
- ✓ *large-area application*
- ✓ *environmentally friendly*
- X *low exciton diffusion length*
- X *low carrier mobility*



# DEVICE PHYSICS



David Beljonne, *Multiscale Modelling of Organic and Hybrid Photovoltaics*, Springer.

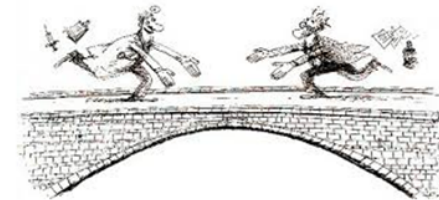




# DEVICE MODEL

Electrodynamics

Semiconductor Physics



**Maxwell's equations**

*Generation rate*

**Poisson equation**

**Drift-diffusion equation  
&  
Current-continuity equation**

**Exciton diffusion-dissociation  
equation**

$$\nabla \times \mathbf{E} = -j\omega\mu_0\mathbf{H}, \quad \nabla \times \mathbf{H} = j\omega\overset{\text{permittivity}}{\varepsilon(\omega)}\mathbf{E}$$

$$\boxed{G(\mathbf{r})} = \int_{400}^{800} \frac{\lambda}{hc} A(\mathbf{r}, \lambda) d\lambda, \quad A(\mathbf{r}, \lambda) = \omega\varepsilon_0 n_r k_i \overset{\text{optical } E\text{-field}}{|\mathbf{E}(\mathbf{r})|^2}$$

*electrostatic potential*

$$\nabla \cdot (\varepsilon \nabla \varphi) = -q(p - n)$$

*electron density*

$$\frac{\partial n}{\partial t} = \eta_d \boxed{G} + \frac{1}{q} \nabla \cdot (q\mu_n n E_n + qD_n \nabla n) + k_d X_l - R(n, p)$$

*hole density*

*mobility*

*diffusion coef.*

*recombination*

$$\frac{\partial p}{\partial t} = \eta_d \boxed{G} - \frac{1}{q} \nabla \cdot (q\mu_p p E_p - qD_p \nabla p) + k_d X_l - R(n, p)$$

*singlet Ex density*

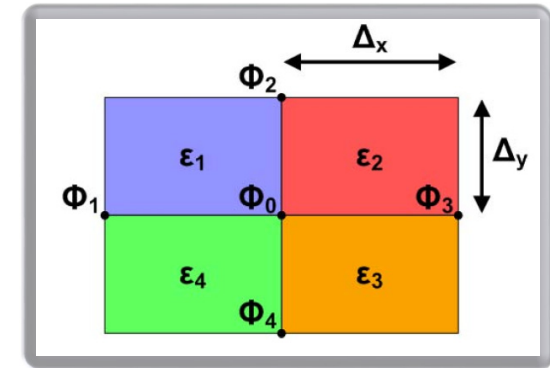
*Ex diffusion coef.*

*Ex dissociation & decay*

$$\frac{\partial X}{\partial t} = (1 - \eta_d) \boxed{G} + \nabla \cdot (D_X \nabla X_l) - k_d X_l - k_f X_l + \eta_s R(n, p)$$

## SOLUTION: SOME REMARKS

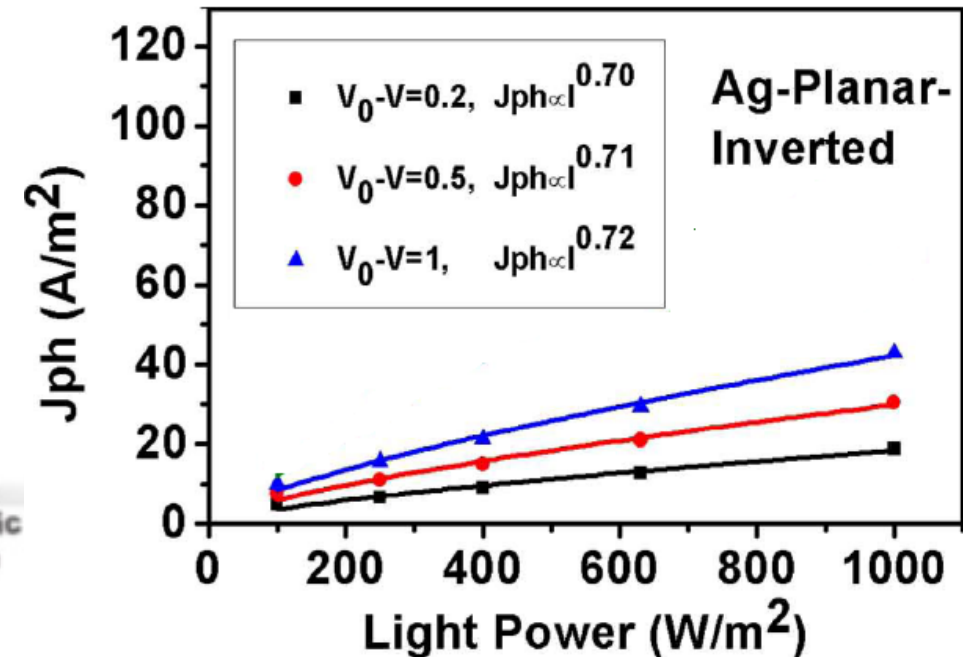
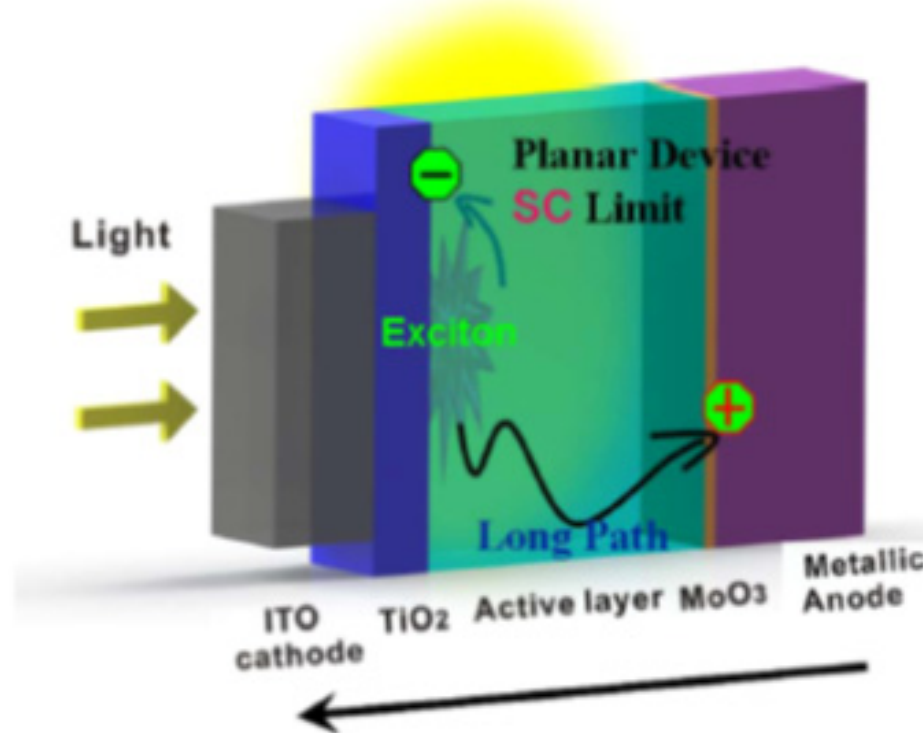
- Unified finite-difference method with identical spatial grids is used. Debye length of organic materials is comparable to decay length of plasmonic waves.
- For Maxwell's equations, frequency-domain or explicit time-domain methods can be employed; For organic semiconductor equations, semi-implicit time-domain method (steady and transient solution) or Newton's method (steady solution) can be adopted.
- For stable multiphysics model, five international units should be redefined.
- Commercial software do not describe exciton behaviors properly.



cm	$\max \{DOS\}^{1/3}$
s	$10^{12}$
V	1
C	$\frac{1}{1.602 \times 10^{-19}}$
K	$\frac{1}{300}$

# SCL FOR PLANAR INVERTED OPVS

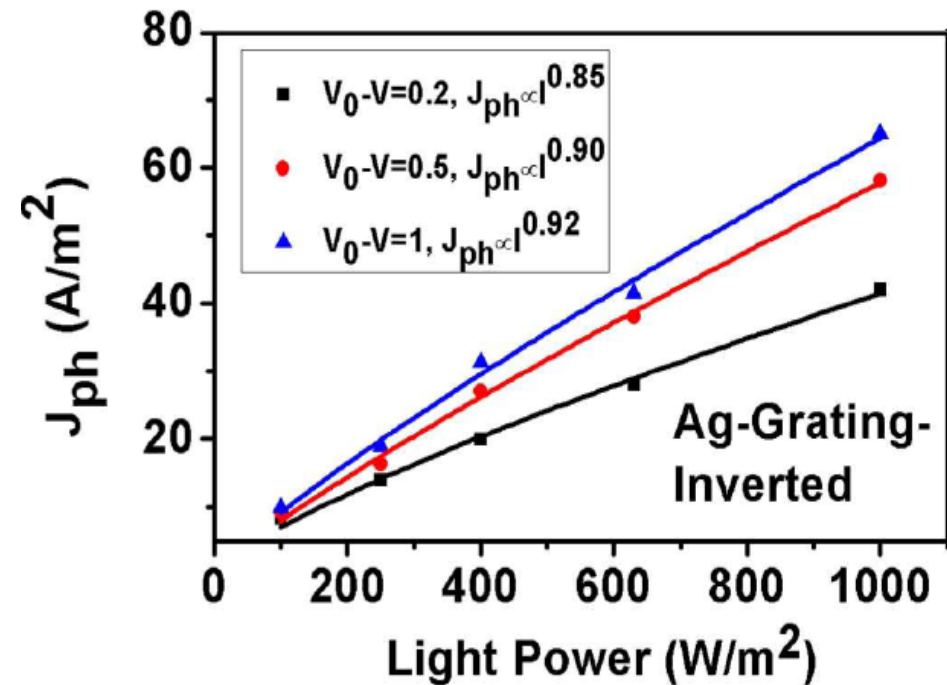
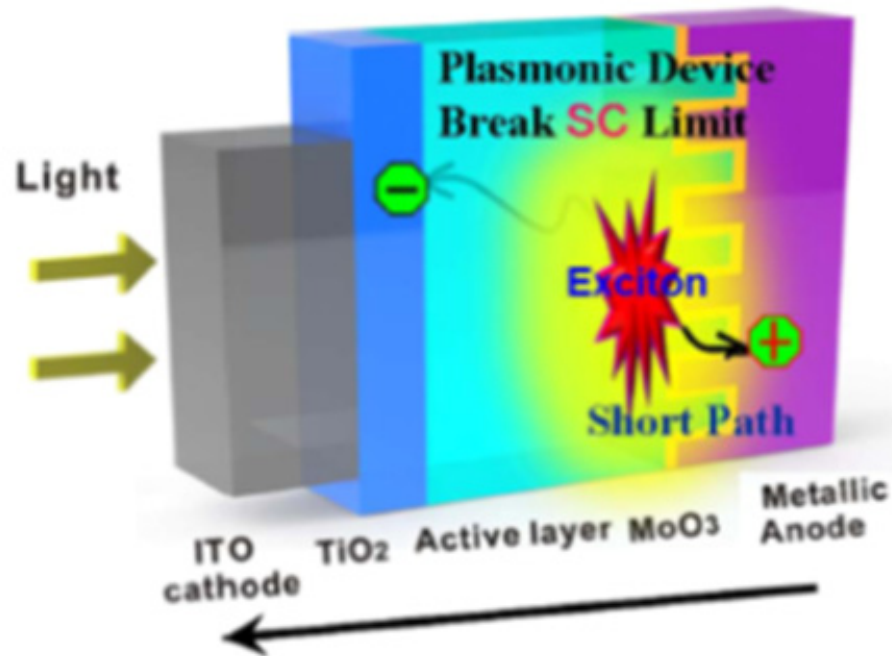
Wei E.I. Sha, Xuanhua Li, and Wallace C.H. Choy, *Scientific Reports*, vol. 4, pp. 6236, Aug. 2014.



Light distribution mainly concentrates around cathode.  
 Low-mobility holes travel a long distance.  
 High-mobility electrons travel a short distance.  
 Space charge limit (SCL) effect occurs.

$$J_{SCL} = q \left( \frac{9\epsilon\mu_h}{8q} \right)^{1/4} G^{3/4} V^{1/2}$$

# SCL BREAKING FOR GRATING INVERTED OPVS



Light distribution concentrates around anode.  
 Low-mobility holes travel a short distance.  
 high-mobility electrons travel a long distance.  
 SCL effect is broken by the plasmonic-electrical effect!

$$J_{normal} = qGL$$

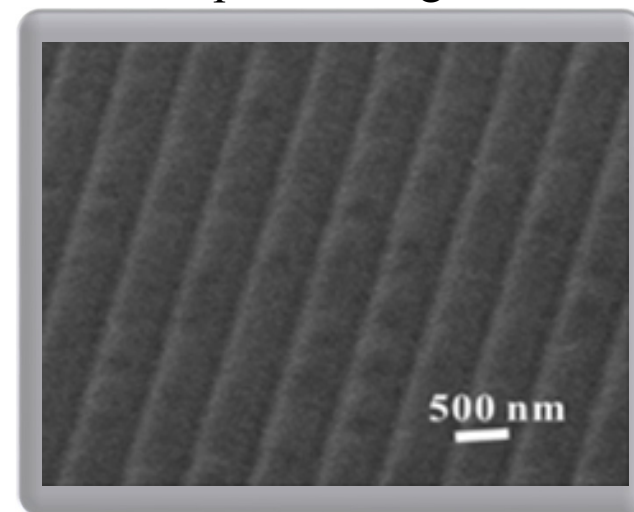
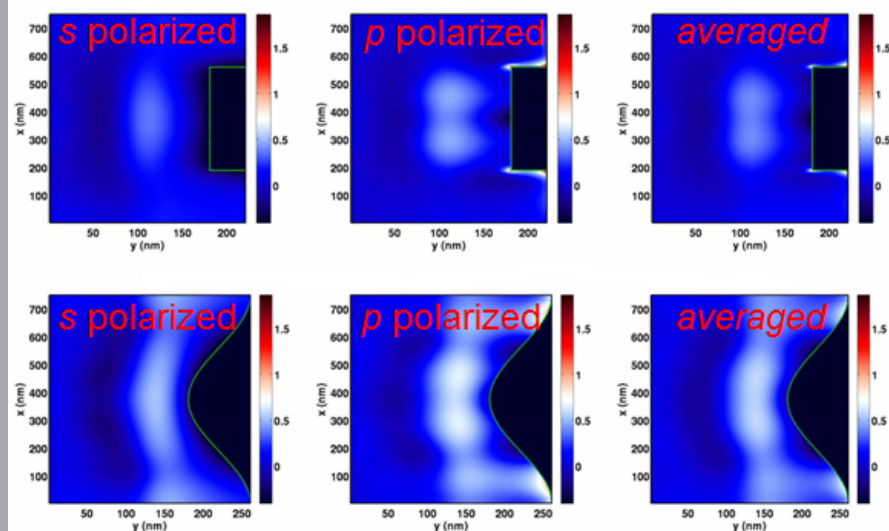




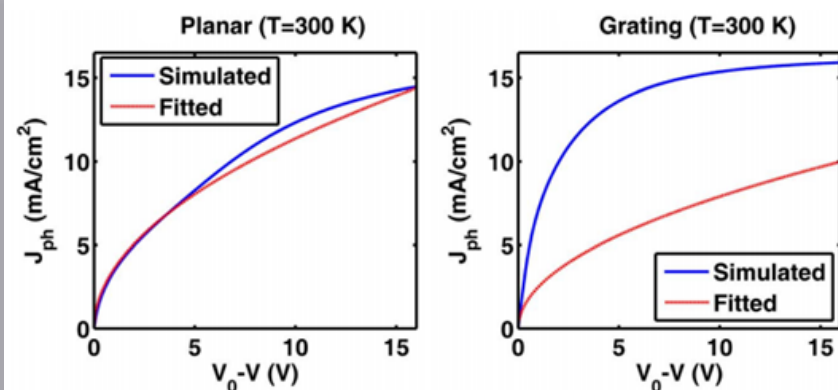
# THEORETICAL RESULTS

exciton generation of grating over that of planar devices

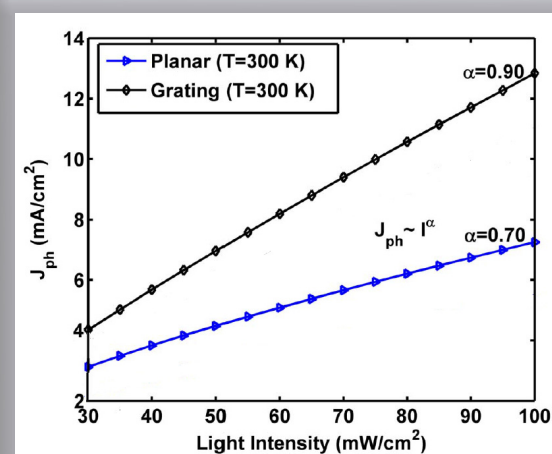
SEM of nanopatterned organic thin-film



current density—voltage curves

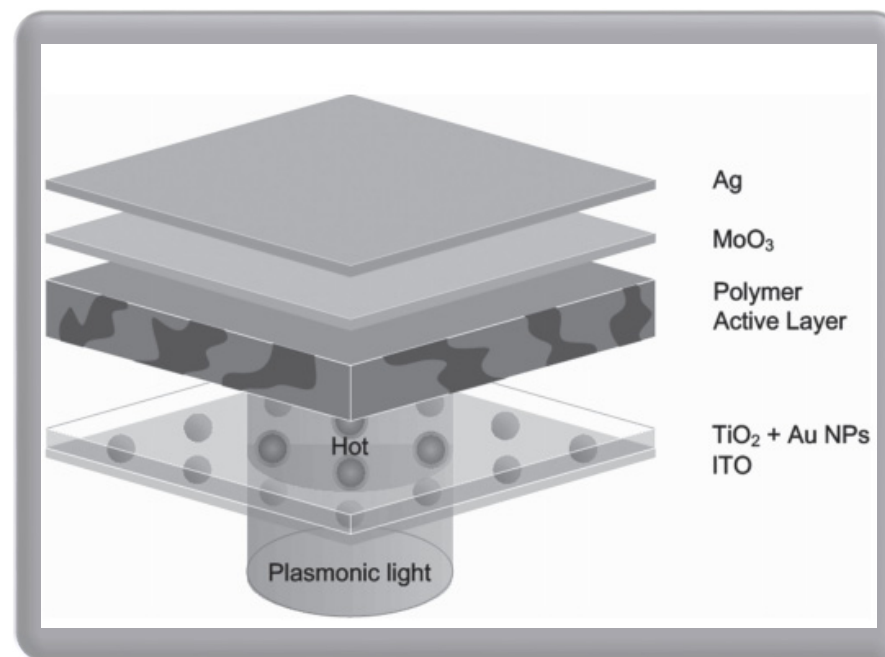
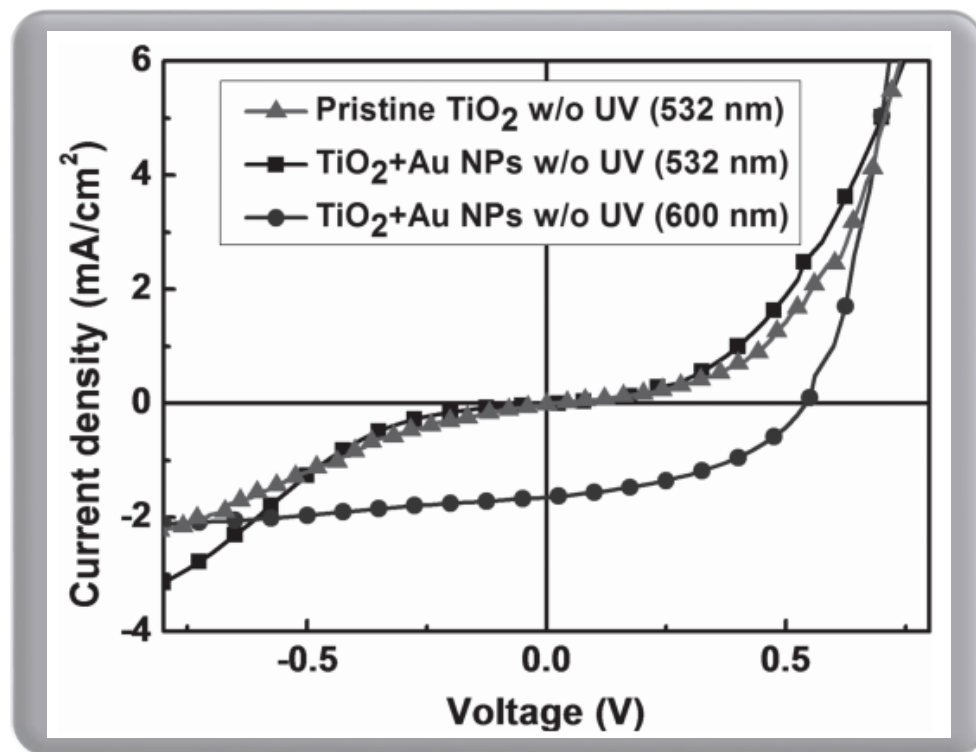


photocurrent—light intensity curves



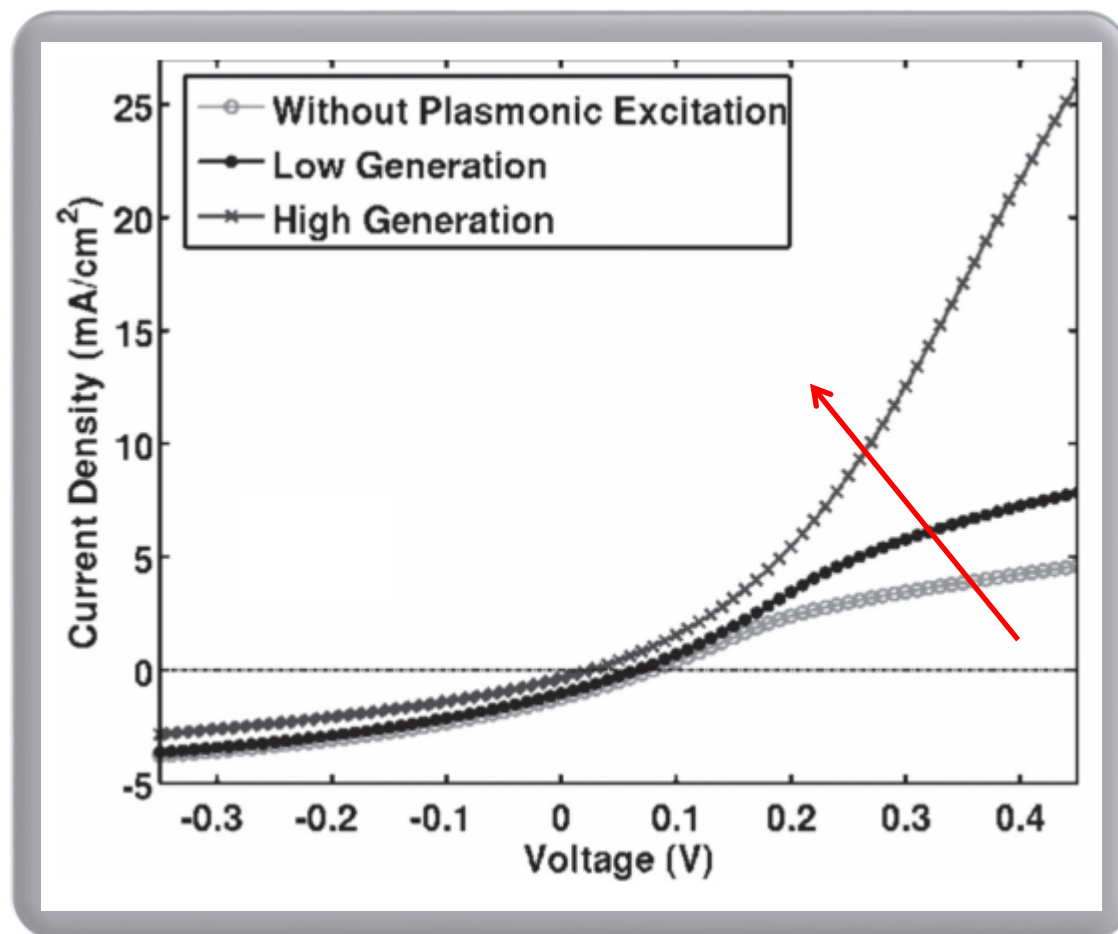
# S-SHAPED $J$ - $V$ CHARACTERISTICS

Di Zhang, Wallace C.H. Choy, Fengxian Xie, Wei E.I. Sha, Xinchun Li, Baofu Ding, Kai Zhang, Fei Huang, and Yong Cao, Wiley, *Advanced Functional Materials*, vol. 23, no. 34, pp. 4255-4261, Sep. 2013.

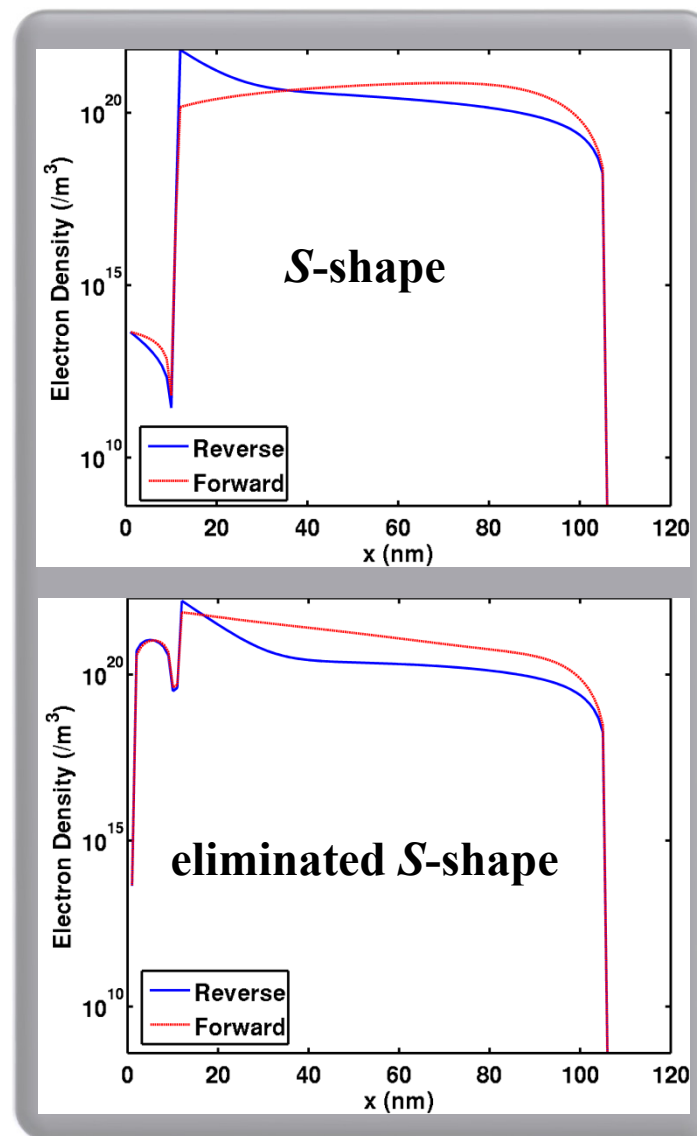


Pristine TiO<sub>2</sub> buffer layer with many trap states induces effective extraction (reverse bias) and injection (forward bias) barriers and thus  $S$ -shaped current density-voltage ( $J$ - $V$ ) curve. On plasmonic resonance, plasmonically excited hot electrons are injected into TiO<sub>2</sub> layer. The injected electrons eliminate the  $S$ -shaped  $J$ - $V$  curve by trap filling and improve charge collection.

# THEORETICAL RESULTS



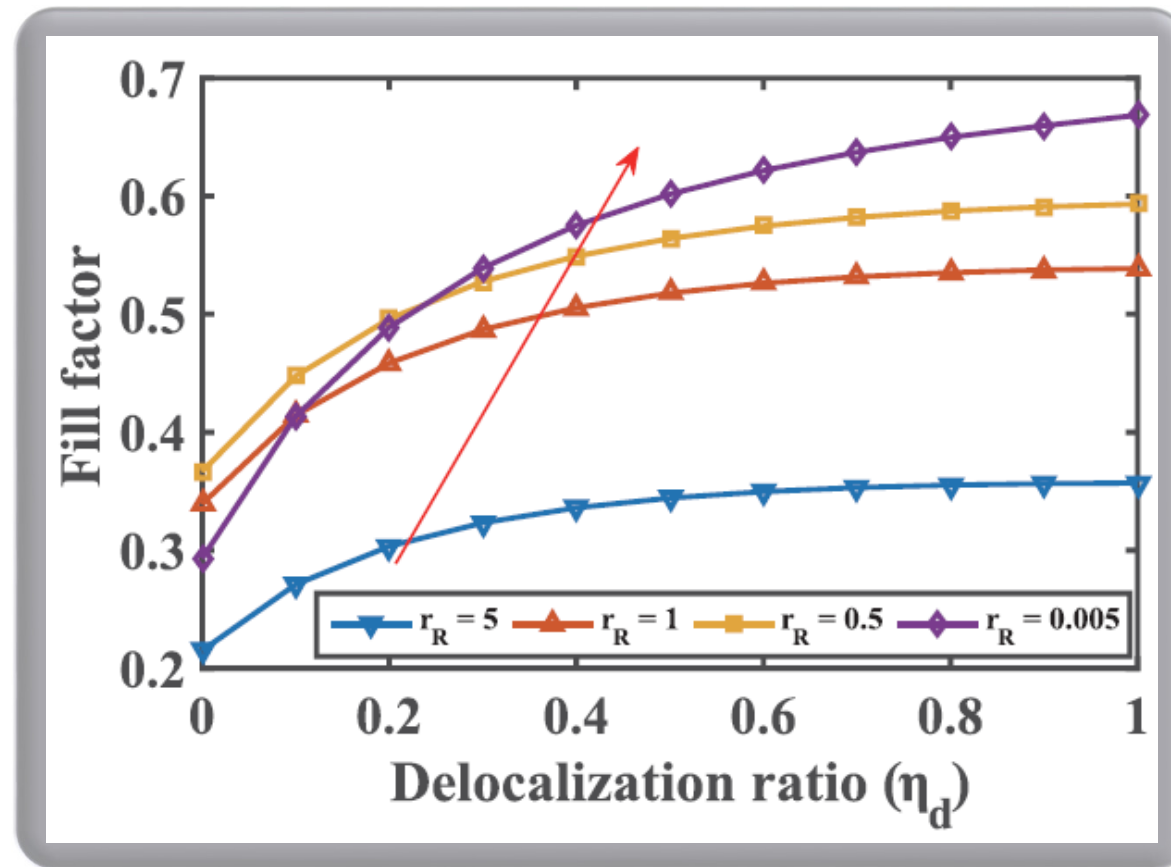
Increasing injected hot electrons will eliminate *S*-shaped *J-V* curve and charge accumulation at the interface will be improved.





# INFLUENCE OF EXCITON DELOCALIZATION

Zi Shuai Wang, Wei E.I. Sha, and Wallace C.H. Choy, "Exciton Delocalization Incorporated Drift-Diffusion Model for Bulk-Heterojunction Organic Solar Cells," *Journal of Applied Physics*, vol. 120, no. 21, pp. 213101, Dec. 2016



The saturation point of fill factor increases when the recombination rate decreases.



# CONCLUSION

1. Device model is fundamentally important to high-performance organic photovoltaics.
2. Optical absorption is governed by Maxwell's equations. Carrier transport is governed by semiconductor equations. Exciton delocalization, diffusion, and dissociation are unique physical processes for organic semiconductor devices, which still need to be carefully studied.
3. Space charge limited current, *S*-shaped *J-V* characteristics, and exciton delocalization induced fill factor saturation in organic solar cells have been theoretically modeled.
4. More multi-physical effects (optical-electrical-thermal-quantum) in photon-carrier interaction will be explored in future works.



# ACKNOWLEDGEMENT



**Any Questions and Discussions?**